## 1] FRICTION AND THERMAL ENERGY

- Until this section, <u>all mechanics is based on the model of object as a single material point</u>. In reality, the objects are constituted by *atoms* (or molecules) which "interact between them and move inside the object" and this means some "energy inside the object". The *atoms* (or molecules) are strongly bound to each other inside a solid, slightly bound between them inside a liquid and they are free (not bound) inside a gaz. But, no matter what is the physical state of object, its *atoms* (or molecules) are in a continuous random motion. This type of motion is characterized by an average speed and this means a kind of kinetic energy inside the object. The temperature of the object is a <u>macroscopic parameter</u> related to the average kinetic energy of atoms (or molecules) inside it. When this type of kinetic energy increases, the temperature of object increases and vice versa. One has labelled as thermal energy "Eth" the amount of energy related to this random motion of microscopic particles inside an object.

Next, one derives the *principle of energy conservation* for a *system* constituted by *objects with microscopic structure*, i.e. a system that contains **thermal energy**.

-One may easily realise (*just by rubbing hands*) that two bodies that rub on each other produce heat. This *heat* <u>increases</u> the <u>thermal energy</u>  $E_{th}$  of the two bodies (*hands get warm*). Precise measurements have shown that the *increase* of *thermal energy of* the two bodies is equal to the *magnitude* of work by friction.

$$\Delta E_{th} (>0) = -W_f = -(-f_k * d) = f_k * d$$
(1)

If the kinetic *friction* is one of external *forces* acting on the *system*, one may separate the work by friction at expression of mechanical energy conservation principle and get  $W_{ext\_net} = W_{ext} + W_f = \Delta E_{mech}$  (2)

Then,  $W_{ext} = \Delta E_{mech} - W_f = \Delta E_{mech} + \Delta E_{th}$  and rewrite the principle of energy conservation as

$$\mathbf{W}_{\text{ext}} = \Delta \mathbf{E}_{\text{mech}} + \Delta \mathbf{E}_{\text{th}} \tag{3}$$

(4)

-Note that  $W_{ext}$  in this expression <u>does not include the work by friction</u>. So, the *external work <u>without</u>* <u>friction work goes</u> for the *change* of *total mechanic energy* of the system **and** the *change* of the *thermal energies* of the system  $\Delta E_{th-sys}$  and that of the external objects  $\Delta E_{th-obj}$  in contact with system parts (fig.1).

 $\Delta E_{th} = \Delta E_{th-sys} + \Delta E_{th-obi}$ 



One may include into system the "*adjacent objects affected by friction*" and make the friction an *internal* <u>*but non-conservative*</u> force of system (fig.2). Then, the expression (3) would tell that net external works (*friction work is not any more external*) goes to change the mechanical and thermal energies of the system.

*Example:* A block with mass m=10kG moving with speed v = 5m/s stops at distance "d" on a horizontal plane that exerts a friction force  $f_k = 5N$  on it. - d —

**—** -

**a**) Find the *change of thermal energy*  $\Delta E_{th}$  of *block - plan set* and **b**) Find "*d* "

If one sees the words *temperature or thermal*, one may *exclude the work by friction from the external* work and refer to the principle energy in form (3).

By excluding the friction from external forces, in this example one get  $W_{ext} = 0$  and the equation (3) gives

 $\Delta E_{mech} + \Delta E_{th} = W_{ext} = 0 \quad or \quad \Delta (U_G + K) + \Delta E_{th} = 0 \quad or \quad \Delta U_G + \Delta K + \Delta E_{th} = 0 \quad and \quad \Delta K + \Delta E_{th} = 0$ because  $\Delta U_G = 0$  (same height) So,  $(0 - 10*25/2) + \Delta E_{th} = 0$  and a)  $\Delta E_{th} = E_{th2} - E_{th1} = 125 J$ b) As,  $\Delta E_{th} = |W_f| = f_k * d$  it comes out that 125J = 5N \* d and d = 25m

Note: The models that take into account the changes in internal energy of objects are used mainly in the frame of thermodynamics. In this course, we refer *mainly* to a system where *friction is an external force*  $(W_f$  is an external work) and use the principle of mechanic energy conservation for a material point model

$$W_{\text{ext\_net}} = \Delta E_{\text{mech}} = \Delta K + \Delta U$$
(5)

One will calculate the total amount of thermal energy produced from the work by friction as  $\Delta E_{th} = -W_f$ .

**Important:** The experiments show that K and U can *transform completely* into each other or into  $E_{th}$ but E<sub>th</sub> cannot transform <u>completely</u> into K or U. A disorganized motion cannot be converted naturally (by itself) into an oriented motion. Ex: A hot block at rest cannot start moving along one direction just because its temperature decreases. That's why the thermal energy is <u>not considered</u> as a pure mechanical energy. Also, one measures the thermal energy (or heat) by a particular unit "calorie" (1 cal = 4.186 J)

## 2] OTHER TYPES OF INTERNAL ENERGY

- Let's consider an *exothermic chemical reaction* inside a sealed container. The molecules "A" interact with molecules "B" at room *temperature* and produce molecules A-B. The chemical reaction releases heat which increases the *temperature* ( $\Delta E_{th} > 0$ ) in container. If the *thermal energy* of particles in sample increases too much, it may be produced an *explosion(and container can break)*. As the system of molecules (A and B) is <u>isolated</u> ( $W_{ext} = 0$ ), the principle of energy conservation (3) would tell that  $\Delta E_{mech} + \Delta E_{th} = 0$  but the experiment shows that  $\Delta E_{mech} > 0$  and  $\Delta E_{th} > 0$ , which means that is  $\Delta E_{mech} + \Delta E_{th} > 0$ . One can avoid this contradiction if one takes into account that there is a *molecular energy* inside each of the molecules in container. One can figure out that the total amount of this type of energy over all molecules in container " $E_{mol}$ " remains constant as long as there is *no chemical reaction*. But, it does change when a chemical reactions happen. So, the total energy of molecules in container is

$$E_{tot} = E_{mech} + E_{th} + E_{mol} \tag{6}$$

Next, the principle of energy conservation for an isolated system would be written  $\Delta E_{tot} = \mathbf{W}_{ext} = \mathbf{0}$ 

 $\Delta E_{mech} + \Delta E_{th} + \Delta E_{mol} = 0 \quad \text{and} \quad \Delta E_{mech} + \Delta E_{th} = -\Delta E_{mol} > 0 \quad i.e. \quad \Delta E_{mol} = E_{mol-2} - E_{mol-1} < 0$ 

This means that, during an <u>exothermic</u> chemical reaction, the amount of energy lost by  $E_{mol}$  part of its internal energy goes to increase the mechanical and thermal energy of the system.

-Inside a battery, the *molecular energy* get transformed (*via a chemical reaction*) into *electrical energy*  $E_{elect}$  which is another type of *internal energy*. There is a set of other *internal energies* ( $E_{struct}$  *in a solid or liquid structure*,  $E_{at}$  - *atomic energy inside the atoms*,  $E_{nucl}$  - *nuclear energy inside the nuclei and*  $E_{rad}$  - *radiation energy*) which cannot transform <u>completely</u> and <u>naturally</u> into <u>pure mechanic energy</u> (K or U). So, they are all *non-mechanical* forms of energy. If one group all them into a single term  $E_{int}$  (*internal energy*), one gets

$$E_{int} = E_{electr} + E_{struct} + E_{mol} + E_{at} + E_{nucl} + E_{rad}$$
(7)

(8)

(10)

and the *total energy* of an object can be expressed as  $E_{tot} = E_{mech} + E_{th} + E_{int}$ 

In mechanics, one prefers to distinguish the term  $E_{th}$  from other terms of  $E_{int}$ .

## 3] GENERAL PRINCIPLE OF ENERGY CONSERVATION

The results of *multiple experiments* confirm the following:

- If one includes *inside a system all the objects that may interact to each other*, one creates an <u>isolated</u> <u>system</u>. The *total energy* of an <u>isolated system</u> remains constant in time i.e.

$$\Delta E_{tot} = \varDelta E_{mec} + \varDelta E_{th} + \varDelta E_{int} = 0 \tag{9}$$

*Note:* This does not exclude motion and energetic exchanges *inside the system; but if they happen, the amount of energy transformed from one form to another is such that the total energy remains constant.* 

- If the system is not isolated the amount of energy that it exchanges with adjacent space regions  $E_{exchange}$ ,

is equal to the change of its total energy  $\Delta E_{tot} = E_{tot-2} - E_{tot-1} = E_{exchange}$ 

If the system *exchanges only work with adjacent space regions*, then  $E_{exchange} = W_{ext}$  (11) and  $W_{ext} = \Delta E_{mech} + \Delta E_{th} + \Delta E_{int}$  (12)

## Remember:

\*The total energy of system increases if  $W_{ext} > 0$  and decreases if  $W_{ext} < 0$ .

\* The work by friction is not included into  $W_{ext}$  at expressions (3, 11, 12).

\*The principle of total energy conservation (12) transforms into form  $W_{ext} = \Delta E_{mech}$  when  $\Delta E_{int} = 0$ .