# **Friction**

#### Purpose:

In this lab, you will measure the coefficients of **static friction** and **kinetic friction** between two combinations of surfaces using an inclined plane.

#### Part 1: Static Friction

#### Theory:

The coefficient of static friction  $\mu_s$  can be measured experimentally for an object (wood block) placed on an inclined plane (ramp). The coefficient of static friction is related to the magnitudes of *maximum friction force f<sub>s-max</sub>* and corresponding normal force N by formula

$$\mu_s = f_{s-\max} / N \qquad (1)$$

In this lab, one increases gradually the friction force  $f_s$  till its maximum value  $f_{s-max}$  by increasing the angle  $\theta$  of an inclined ramp shown in figure. One measures the angle  $\theta = \theta_s$  at the moment the block just start to slide and calculates the static friction coefficient as

$$\mu_s = \tan \theta_s$$
 (2)

One can get expression (2) by writing the second law for the block just before it starts to slide

$$\overrightarrow{F_G} + \overrightarrow{f_{s-max}} + \overrightarrow{N} = m\overrightarrow{a} = 0$$

After projecting it on Ox, Oy axes, one get

Ox:  $+F_G \sin\theta_s - f_{s-max} = 0$  *i.e.*  $f_{s-max} = F_G \sin\theta_s$  and Oy:  $-F_G \cos\theta_s + N = 0$  *i.e.*  $N = F_G \cos\theta_s$ Finally  $f_{s-max} = F_G \sin\theta_s = \mu_s N = \mu_s F_G \cos\theta_s$  and  $\mu_s = tan\theta_s$ 

This last relation allows to calculate the static friction coefficient by the smallest value of angle  $\theta_s$  for which the bloc just starts sliding.



## Equipment:

For this lab, you will use an inclined ramp, a wooden block with "two different materials on surface" and a towel paper.

# **Experiment#1: Measuring static friction coefficient**

- 1. Cover the ramp by a piece of towel paper and draw a line on it upper side.
- 2. Place the block on the paper and align its upper side to the line.
- 3. Increase carefully the ramp angle till the block starts sliding and measure the angle  $\theta_s$ .
- 4. Note the angle in the table 1.
- 5. Repeat three to five times the measurement and include angles values in the table.
- 6. Calculate the best, max and min estimated values for  $\theta_s$  (two types of uncertainty involved).
- 7. Use expression (2) to calculate the best, max and min estimations values for  $\mu_s$ .

Tab#2

- 8. Repeat the same steps for the smaller area of block having the same material.
- 9. Fill tab#2 with those data and calculate best, max and min estimated values.

10. Verify whether the friction force on the block depends on the area of surfaces in contact.

## Contact surface: \_\_towel paper- smooth wood

Large contact area

Small contact area

Tab#1

	$\theta_s$	$\mu_{s}$
First		
Second		
Third		
Fourth		
Fifth		
Best		
Max		
Min		

	$\theta_s$	$\mu_{S}$
First		
Second		
Third		
Fourth		
Fifth		
Best		
Max		
Min		

Next, you repeat those measurements for the other contact surface of the block and the towel paper and fill tables 3 and 4.

# Contact surface: \_\_towel paper - rugged surface

Large contact area Tab#3

	$\theta_{s}$	μs
First		
Second		
Third		
Fourth		
Fifth		
Best		
Max		
Min		

Small contact area Tab#4

	$\theta_s$	μs
First		-
Second		
Third		
Fourth		
Fifth		
Best		
Max		
Min		

## Part 2: Kinetic Friction

#### Theory:

One can measure the coefficient of kinetic friction,  $\mu_k$ , by using the same method used for the coefficient of static friction by referring to a situation where the *block is sliding at constant velocity*, i.e. **zero acceleration**. In this case, though, one must make sure that, once starting to slide, the block will follow sliding uniformly. This situation corresponds to a precise inclination angle  $\theta = \theta_k$  and

 $\mu_k = \tan \theta_k$  (3)

## **Experiment:**

You can measure  $\mu_k$  using a procedure similar to the one you used to measure  $\mu_s$ . This time, just pick one area (say the large one) for each of two combinations of different surfaces in contact.

- 1. Place the block on the towel paper at smallest inclination and give it a small push. The block will stop after a small displacement.
- 2. Increase slowly the plane inclination and repeat the point 1 each time. At a given angle, the block will not stop; it will slide until the end of inclined plan. Here we are dealing with a uniform motion. You have to measure the smallest angle  $\theta_k$  for which this happens and write it in table 5. *Question: Why do we have to refer to the smallest angle?*
- 3. Repeat three to five times steps 1-2 and record in table 5 the found values for the angle  $\theta_k$ . Use the relation (3) you derived above in order to calculate the coefficient of kinetic friction  $\mu_k$ .
- 4. Repeat the steps 1 to 3 for the other set of surfaces in contact and fill the table 6.

Contact surface: *towel paper-smooth wood* 

towel paper - rugged surface

Tab#5

	$\theta_k$	$\mu_k$
First		
Second		
Third		
Fourth		
Fifth		
Best		
Max		
Min		

Tab#6

	$\theta_k$	$\mu_k$
First		
Second		
Third		
Fourth		
Fifth		
Best		
Max		
Min		

#### Analysis:

Use the following questions to write a meaningful analysis. (Don't answer them in a "telegraphic way")

- 1. Why do you have to include the two types of uncertainty in calculations for  $\theta$ ?
- How do the values of μ<sub>s</sub> compare to the values of μ<sub>k</sub>?
  (Of course, you can only compare them for the same pairs of materials.)
- 3. Do these values  $\mu_s$  and  $\mu_k$  fit to what you expected?
- 4. Do the friction coefficients  $\mu_s$  and  $\mu_k$  depend on the nature of surfaces in contact? Explain.
- 5. Of the two parts of the experiment, measurement of  $\mu_s$  and measurement of  $\mu_k$ , which one had more possible sources of uncertainty ? Explain.
- 6. Could  $\mu_k$  or  $\mu_s$  ever be greater than 1? Explain why or why not.
- 7. Does the coefficient of friction depend on the size of the contact area or not?